



# Elastography in deformed viscoelastic strips

A. DELORY<sup>1,2</sup>, D. KIEFER<sup>1</sup>, M. LANOY<sup>1,3</sup>, A. EDDI<sup>2</sup>, C. PRADA<sup>1</sup> & F. LEMOULT<sup>1</sup>



GdR MecaWave – May 9, 2022

<sup>1</sup> Institut Langevin, ESPCI Paris, Université PSL, CNRS, Paris, France

<sup>2</sup> PMMH, ESPCI Paris, Université PSL, Sorbonne Université, Paris

<sup>3</sup> LAUM, IA-GS, CNRS, Le Mans Université, Le Mans, France



Evaluating the body resistance (Young's modulus  $E$ )

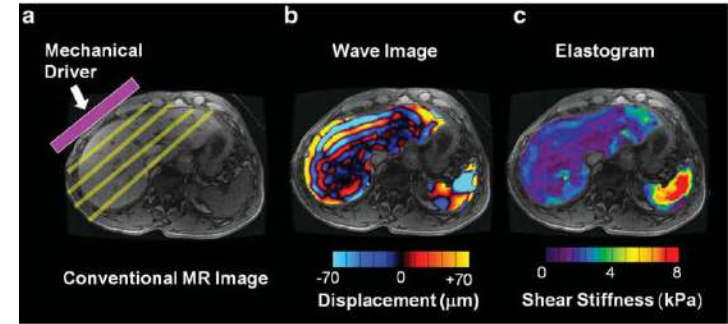


From Wikipedia "Doctor Murai Kinzan's teachings (alias Genshinkan, 1733-1815)" Collection W. Michel (Fukuoka, Japan)  
Sandrin et al. "Non-Invasive Assessment of Liver Fibrosis by Vibration-Controlled Transient Elastography (Fibroscan®)" (2011)  
Formation Pole Therapeutes "L'importance de la palpation abdominale et des fascias au cœur de la formation techniques-manuelles"



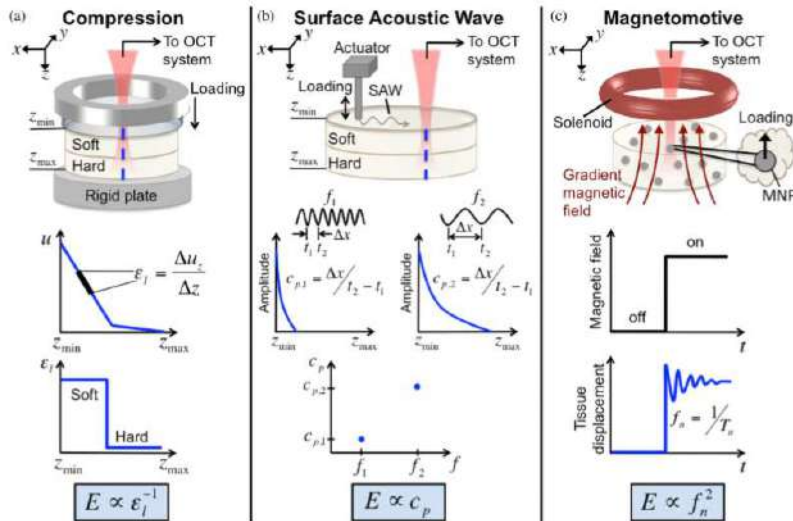
Field of view ↑

Measuring shear wave velocity:  
 $E = 3 \times \rho V^2$



MRE

OCE



→ Spatial resolution

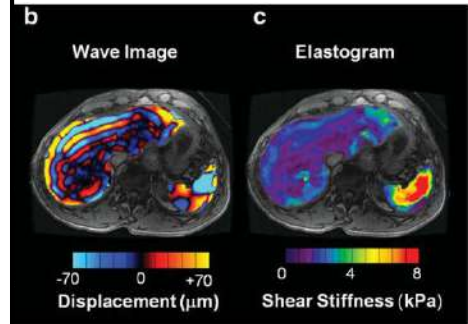
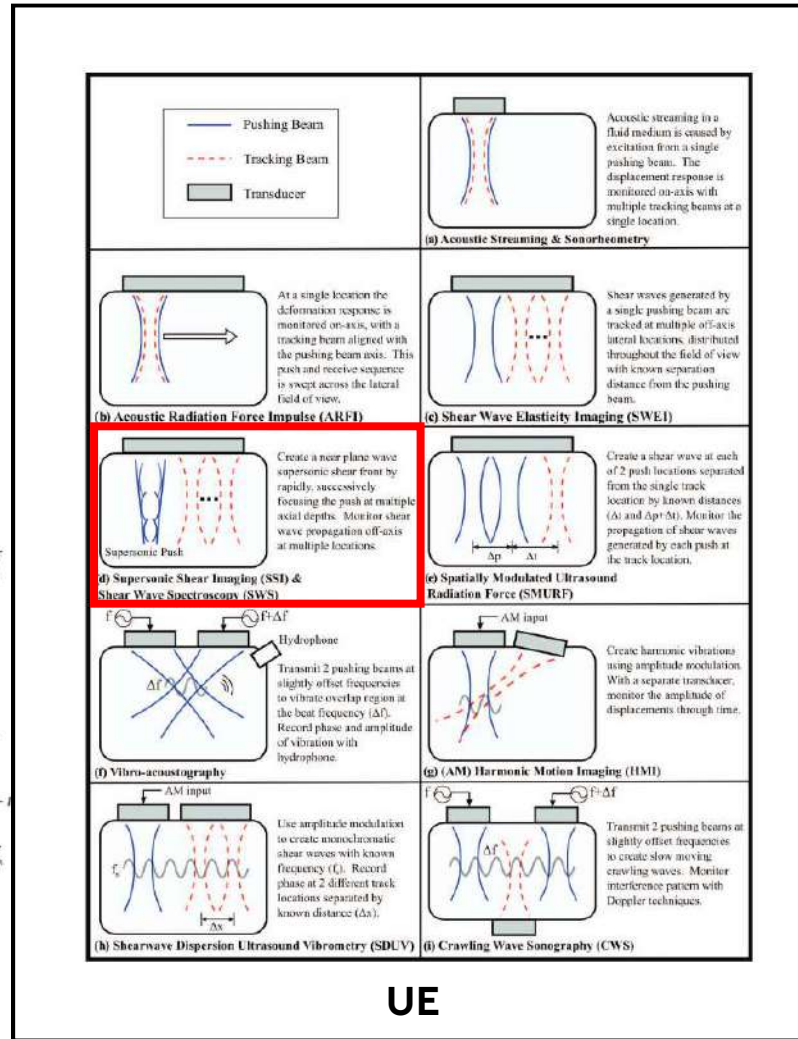
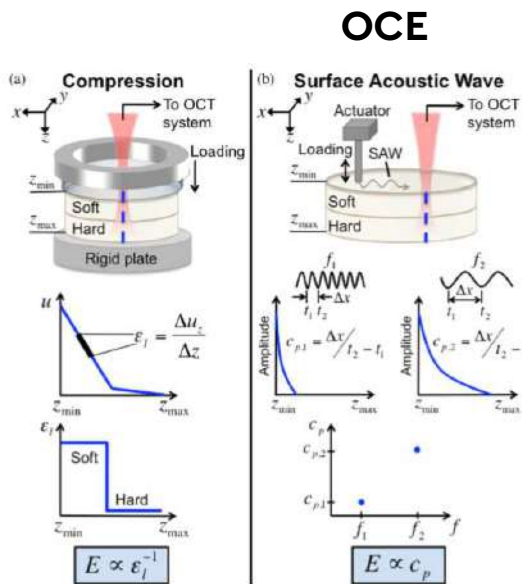
Venkatesh et al "Magnetic resonance elastography of liver: Technique, analysis, and clinical applications" in JMRI, **37** (2013)  
 Kennedy et al. "A Review of Optical Coherence Elastography: Fundamentals, Techniques and Prospects" in IEEE JSTQE, **20**, 2 (2014)  
 Doherty et al. "Acoustic radiation force elasticity imaging in diagnostic ultrasound" in IEEE TUFFC, **60**, 4 (2013)





Field of view

Measuring shear wave velocity:  
 $E = 3 \times \rho V^2$



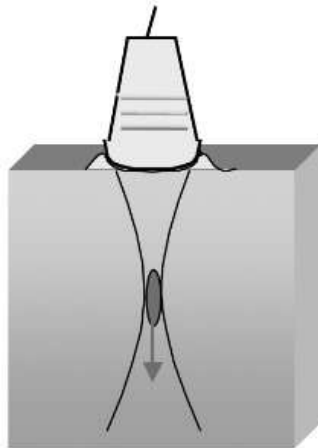
**MRE**

Spatial resolution

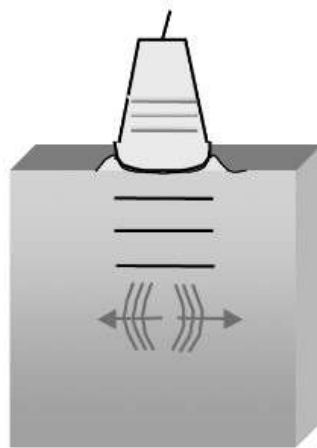
Venkatesh et al "Magnetic resonance elastography of liver: Technique, analysis, and clinical applications" in JMRI, **37** (2013)  
 Kennedy et al. "A Review of Optical Coherence Elastography: Fundamentals, Techniques and Prospects" in IEEE JSTQE, **20**, 2 (2014)  
 Doherty et al. "Acoustic radiation force elasticity imaging in diagnostic ultrasound" in IEEE TUFFC, **60**, 4 (2013)



Pushing mode



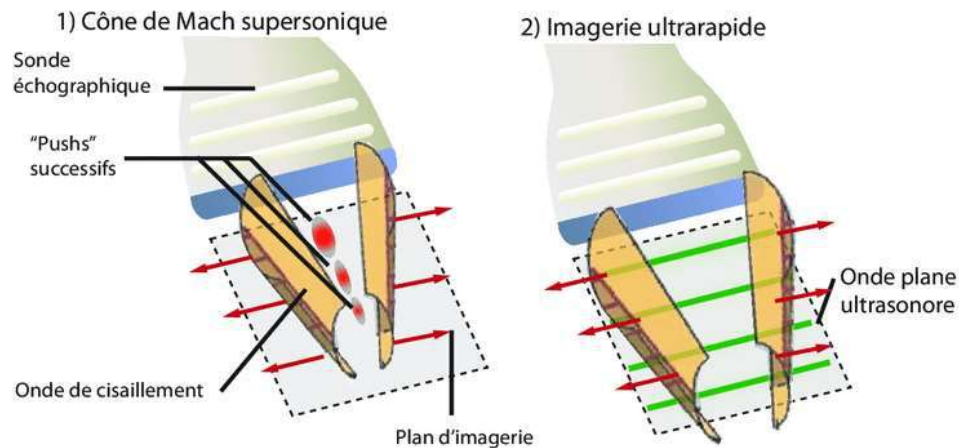
Imaging mode



Measuring  
shear wave  
velocity:  
 $E = 3 \times \rho V^2$

Some limitations for robust  
quantitative elastography:

- Waveguide geometry
- Anisotropy
- Viscoelasticity
- Prestress

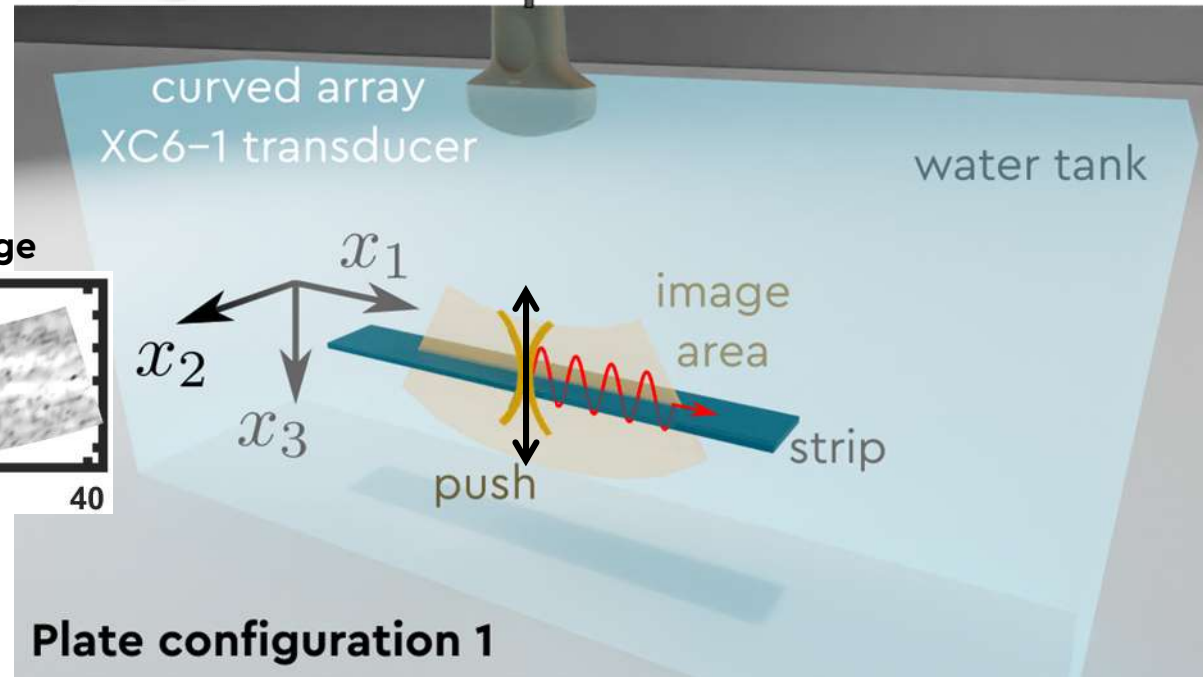
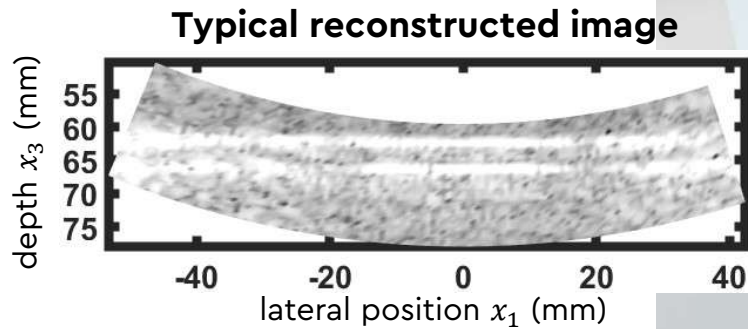
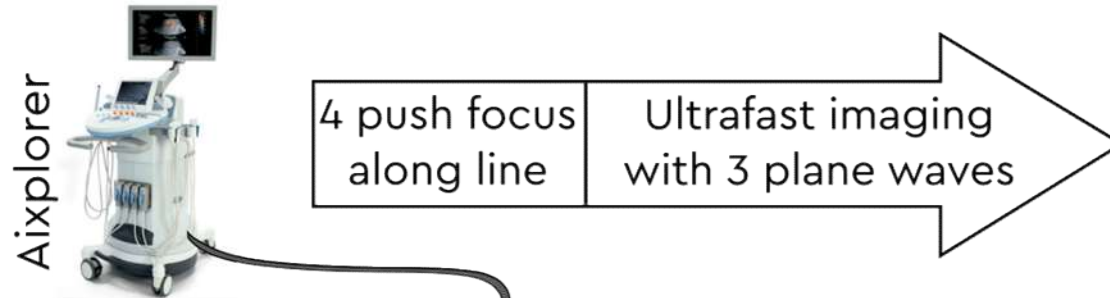


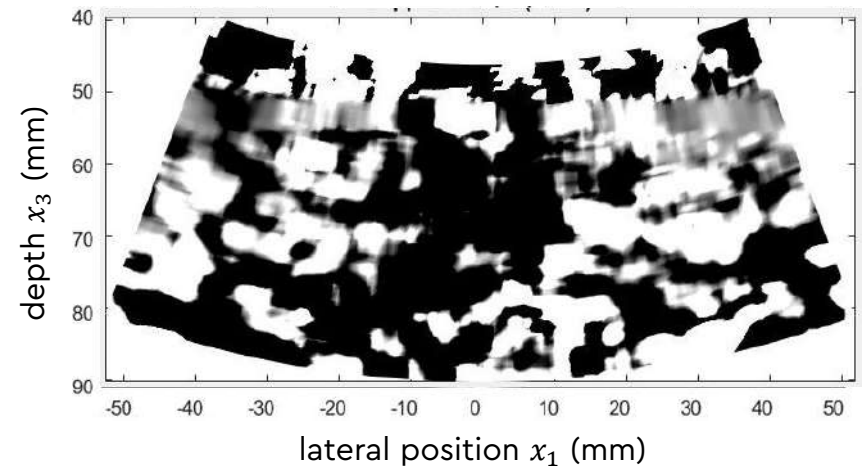
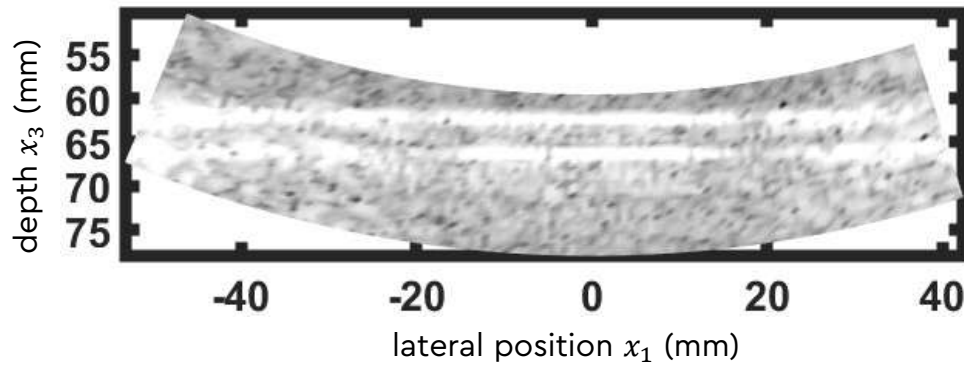
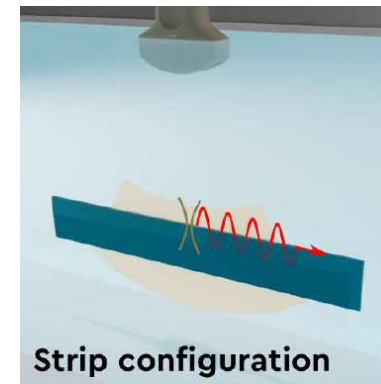
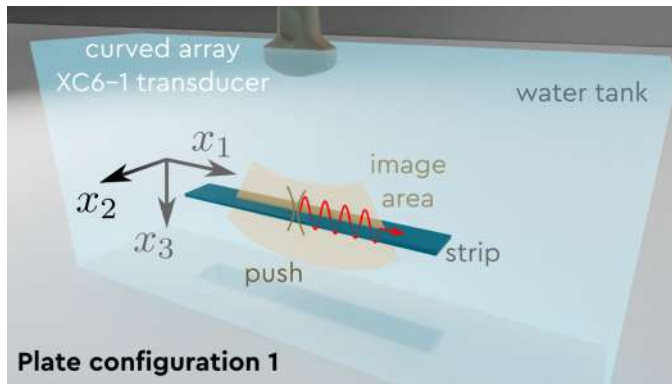
Bercoff et al. "Supersonic shear imaging" IEEE TUFFC, **51**, 4 (2004)  
Deffieux PhD (2008)

Bilston, NMR in Biomedicine, **31**, 10 (2018)  
Sigrist et al., Theranostics, **7**, 5 (2017)

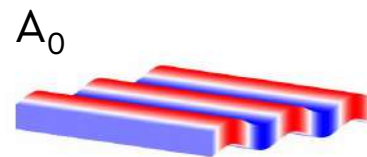
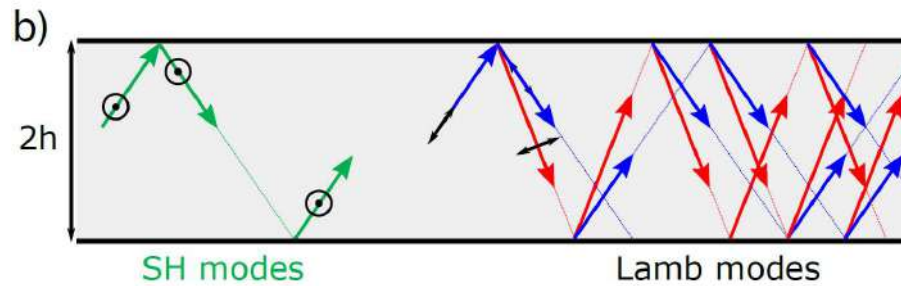
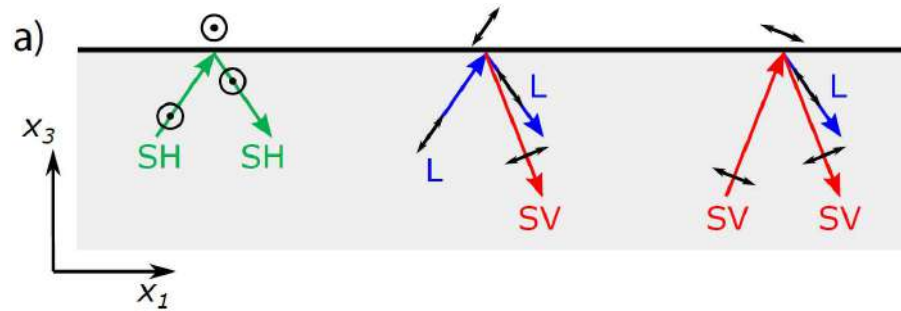


EcoFlex® = silicon gel

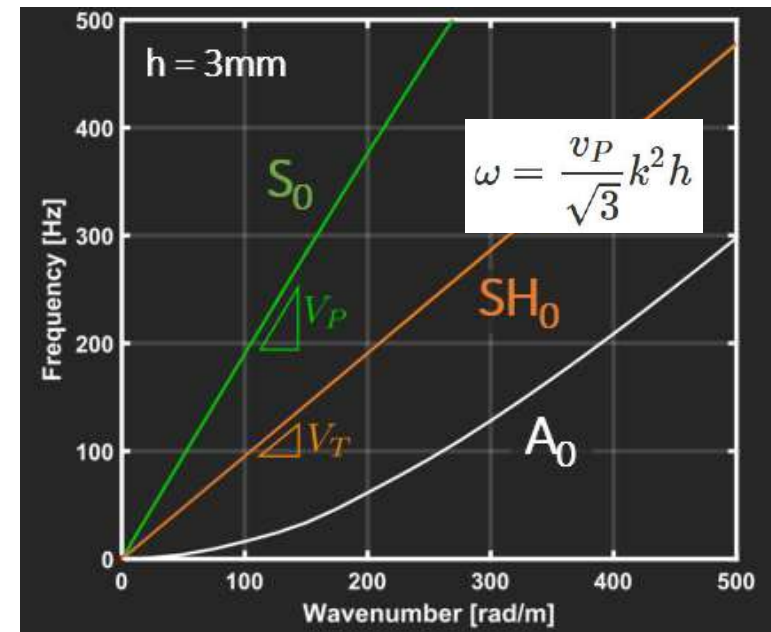






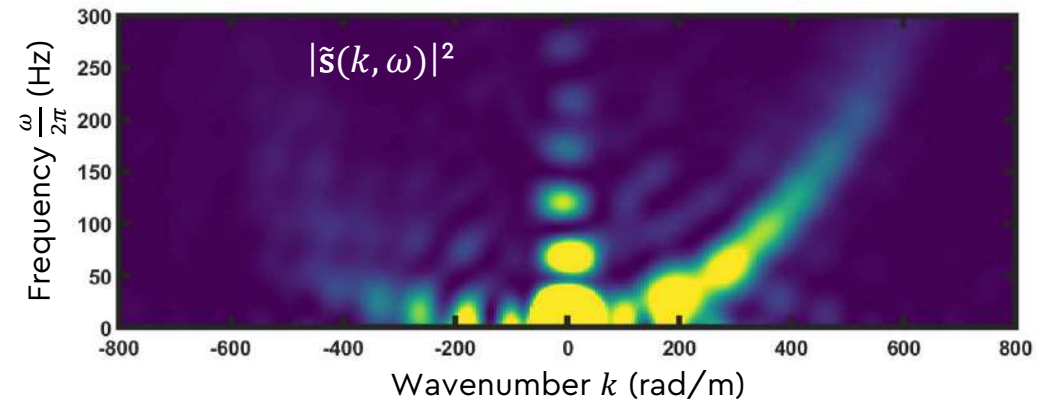
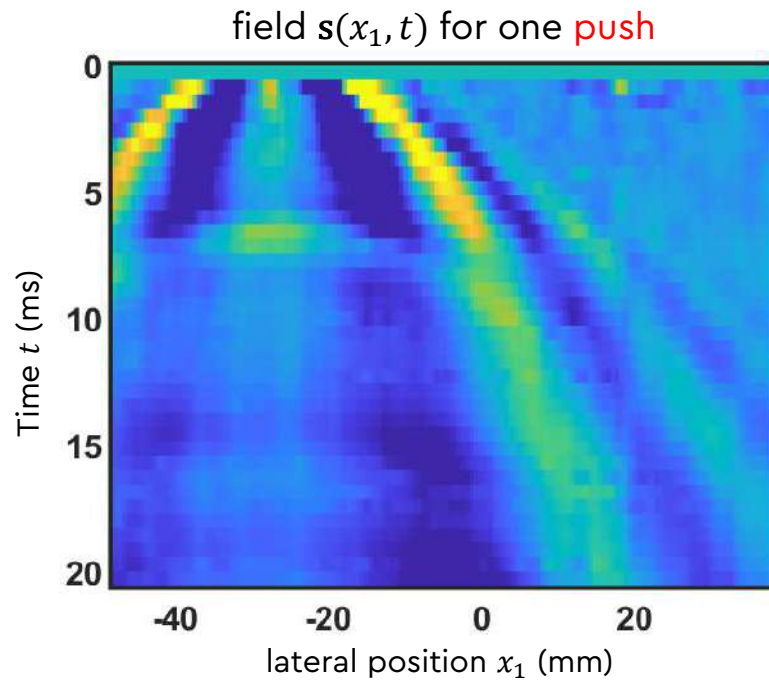
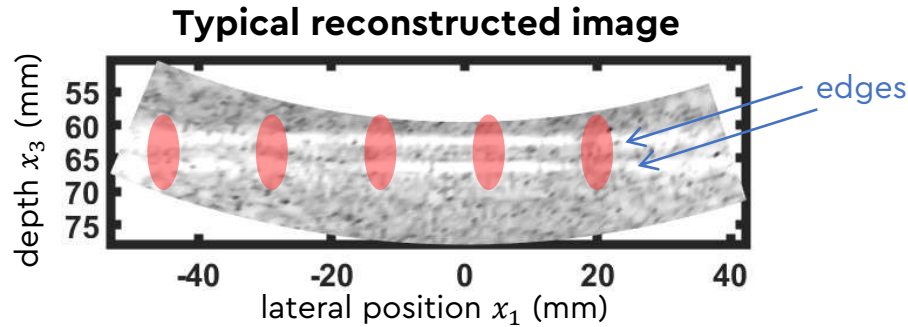
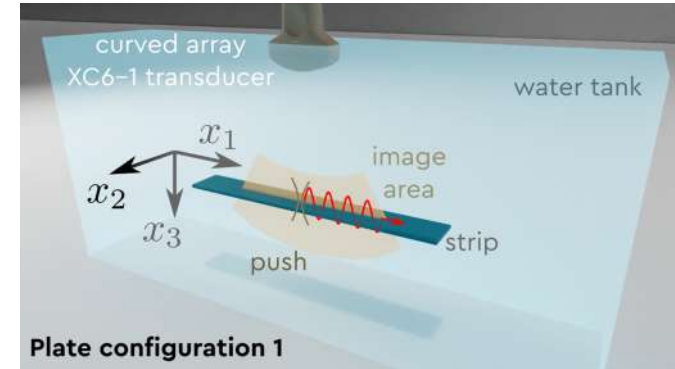


Theoretical dispersion curves



Delory, Lemoult, Lanoy, Eddi & Prada. "Soft elastomers: A playground for guided waves", JASA **151** (2022)

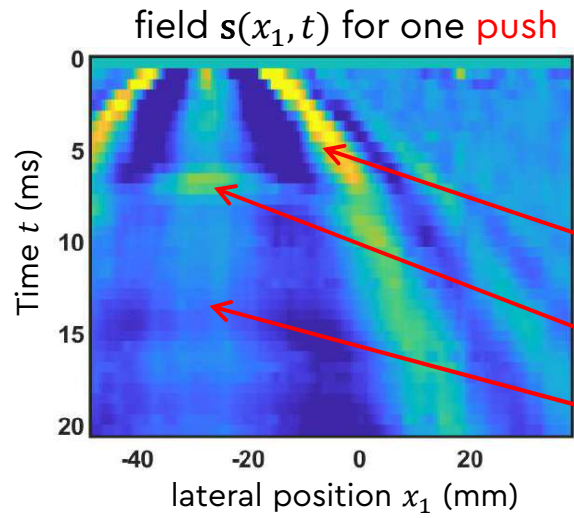
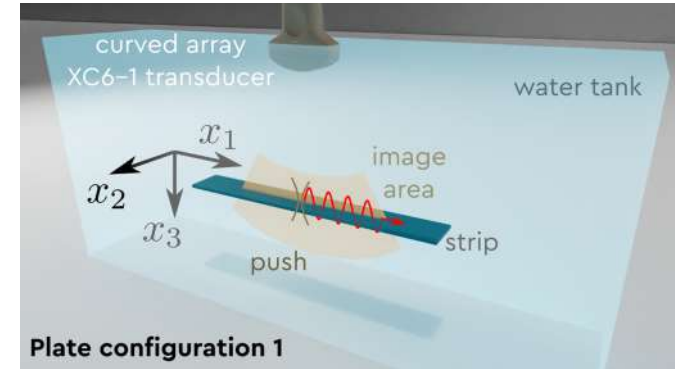




→ Push at different locations and superimpose dispersion curves

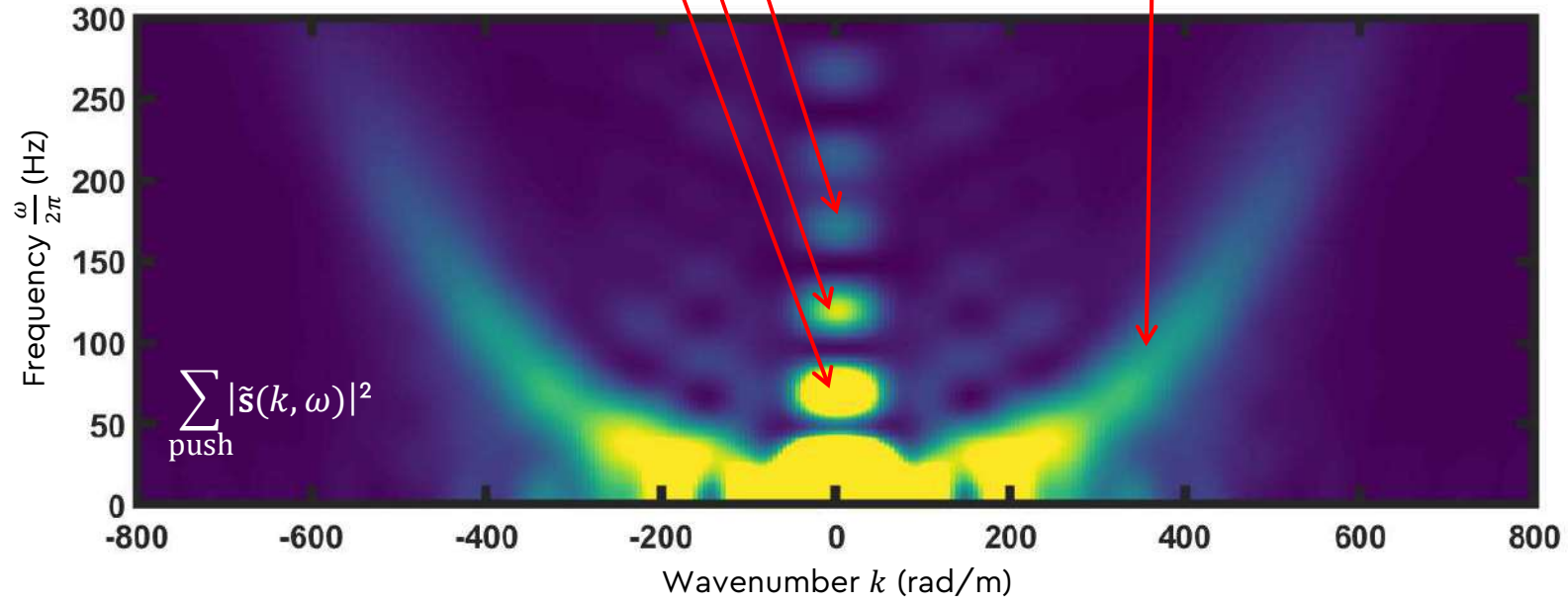


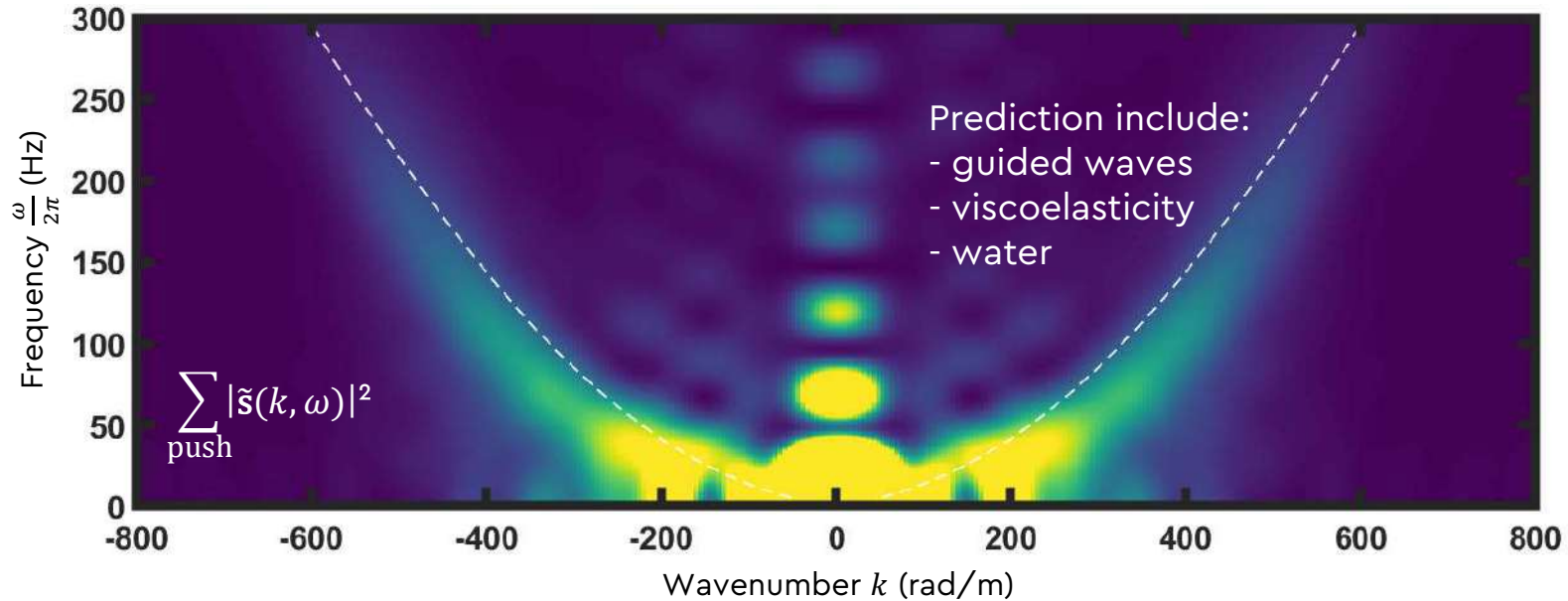
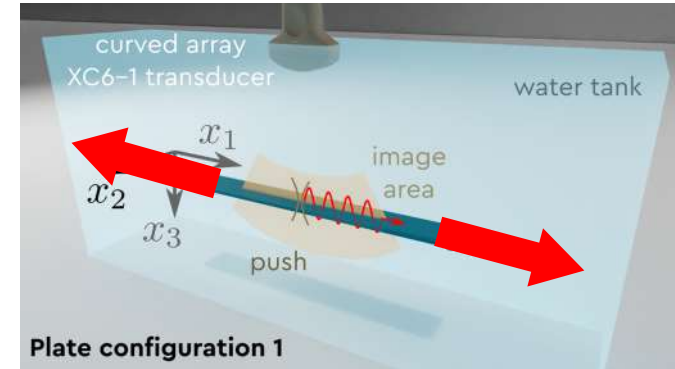
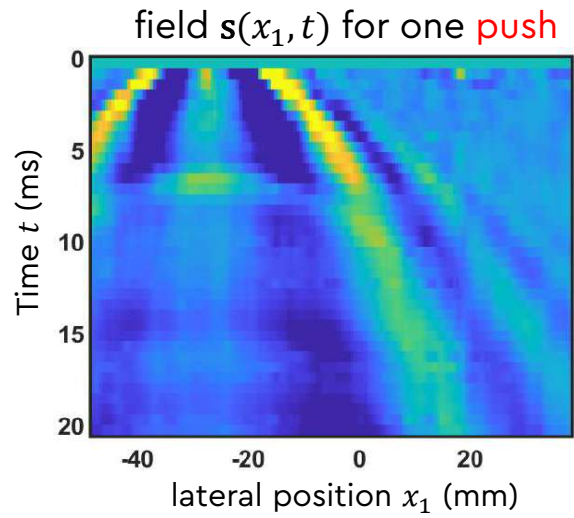
# Results in the undeformed strip

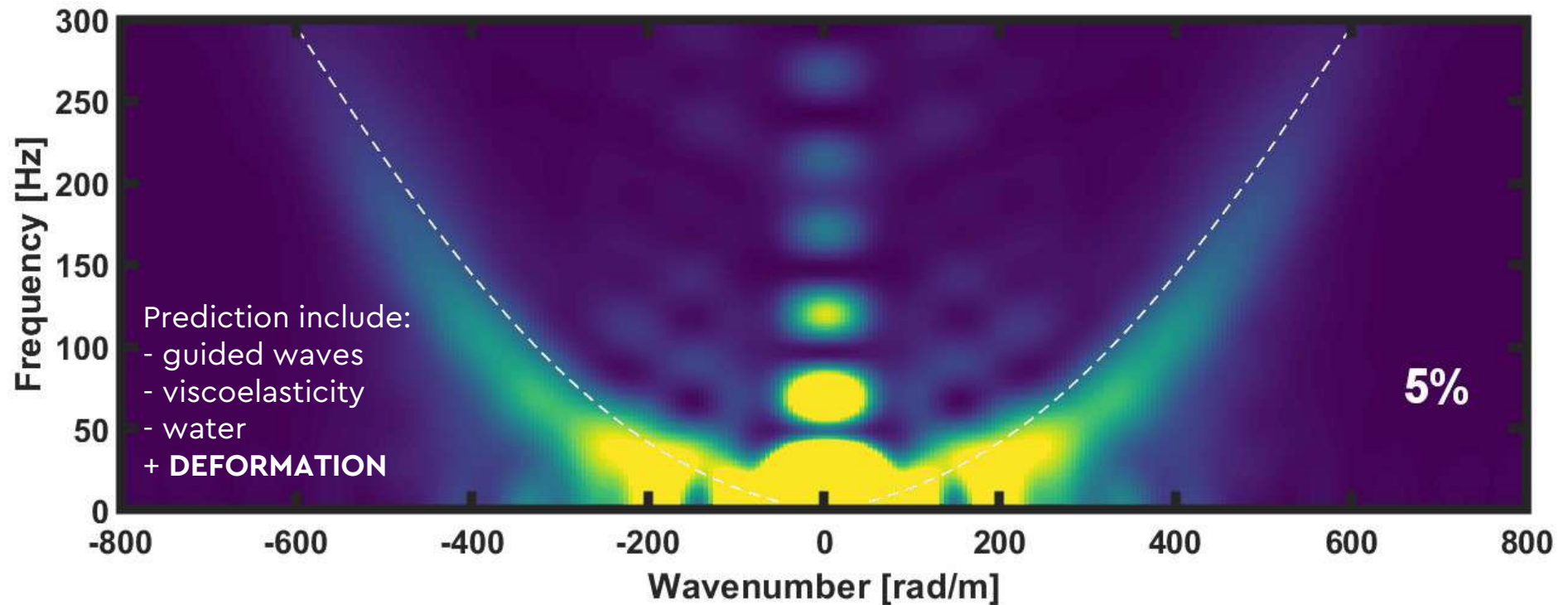


Back and forth  
along the width  $x_2$

Propagation of  
quasi- $A_0$  (in water)







To take deformation into account, use an equivalent elasticity tensor:

$$C_{jkl}^{\omega} \frac{\partial^2 u'_l}{\partial x_j \partial x_k} = \rho \frac{\partial^2 u'_i}{\partial t^2}$$

$$C_{ijkl}^{\omega} = C_{ijkl}^0 + (\delta_{ik} \delta_{jl} + \delta_{il} \delta_{kj}) \left( \nu + \beta \frac{\lambda_i^2 + \lambda_j^2}{2} \right) (i\omega)^n$$

Eulerian elasticity tensor  
for a Mooney-Rivlin solid

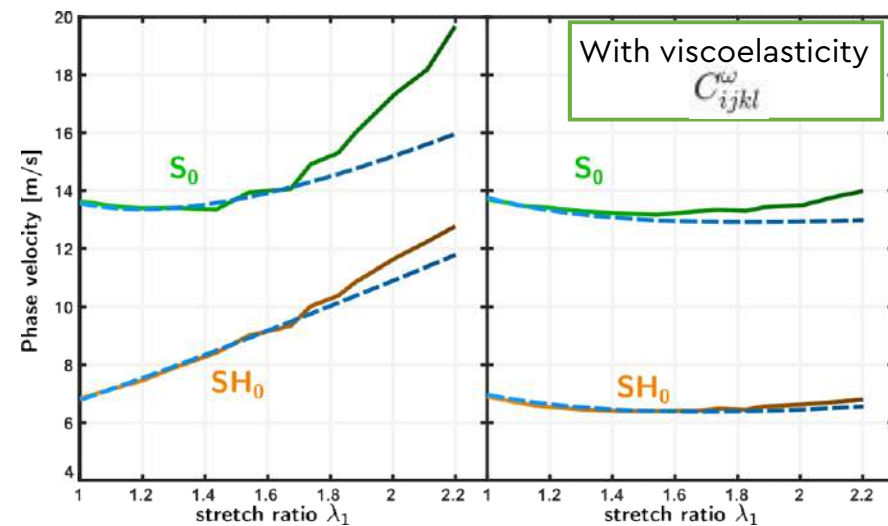
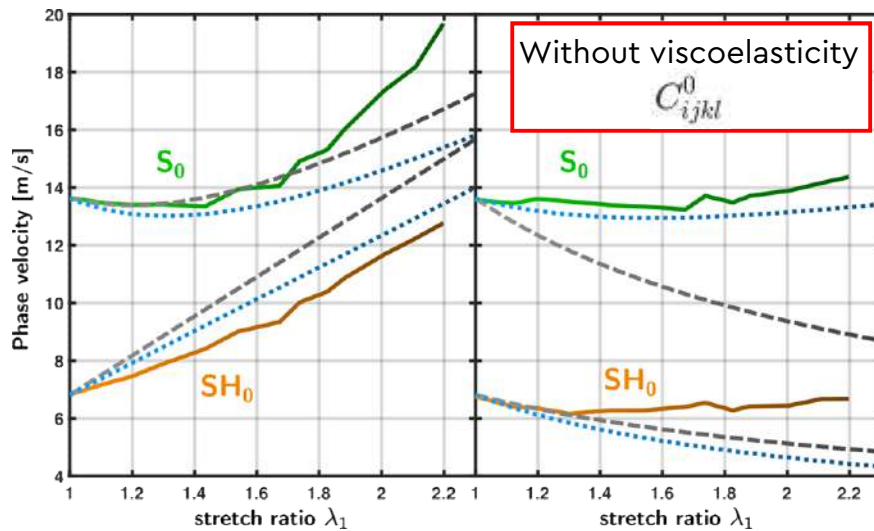
Shear motion

Viscoelastic non-linearity

Fractional  
KV model

Delory, Lemoult, Eddi & Prada. "Guided elastic waves in a highly-stretched soft plate", EML 61 (2023)





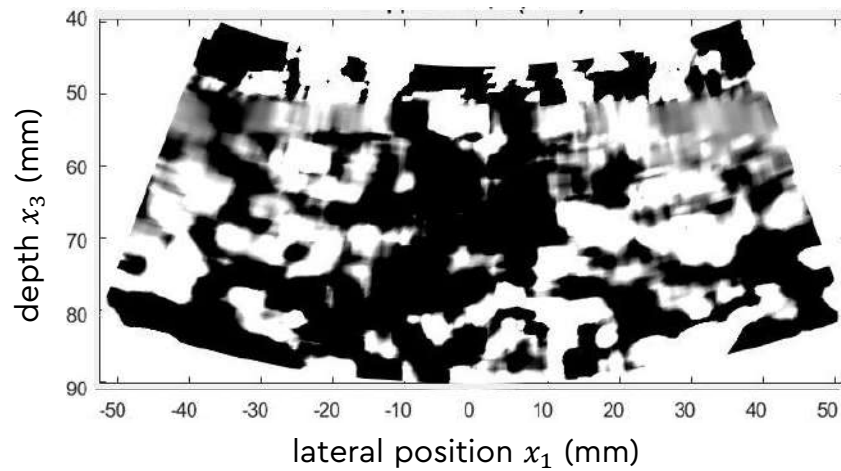
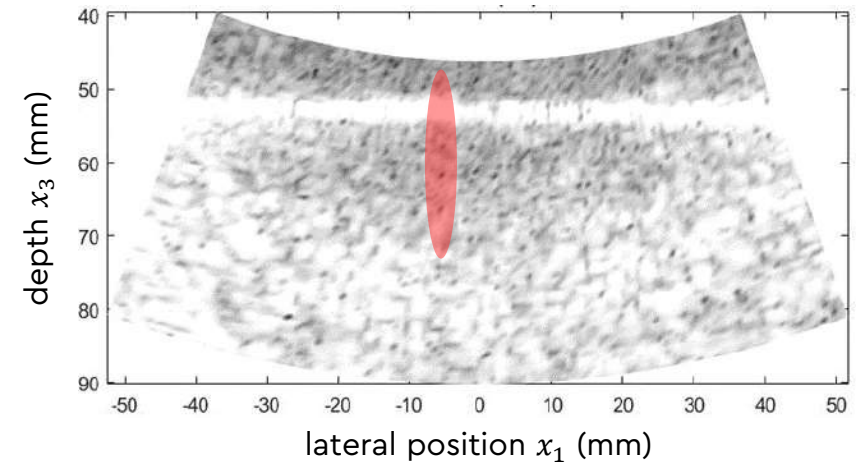
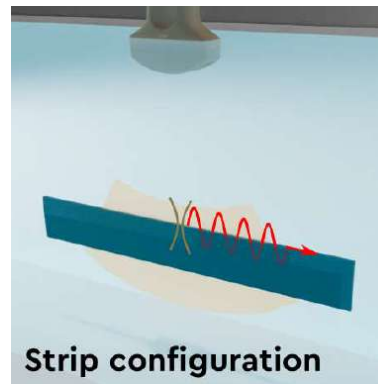
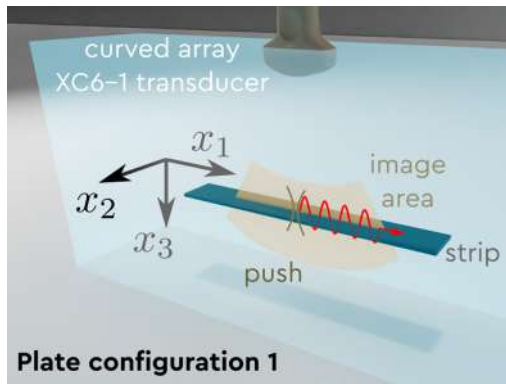
Taking into account the viscoelastic model of our material:

$$\mu(\omega) = \mu_0 [1 + (i\omega\tau)^n]$$

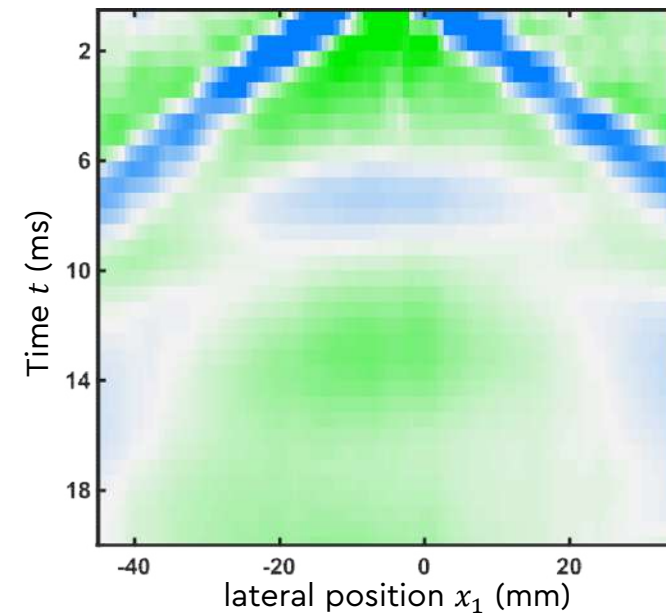
↓  
Fitting for  $\beta'$  and  $\alpha$

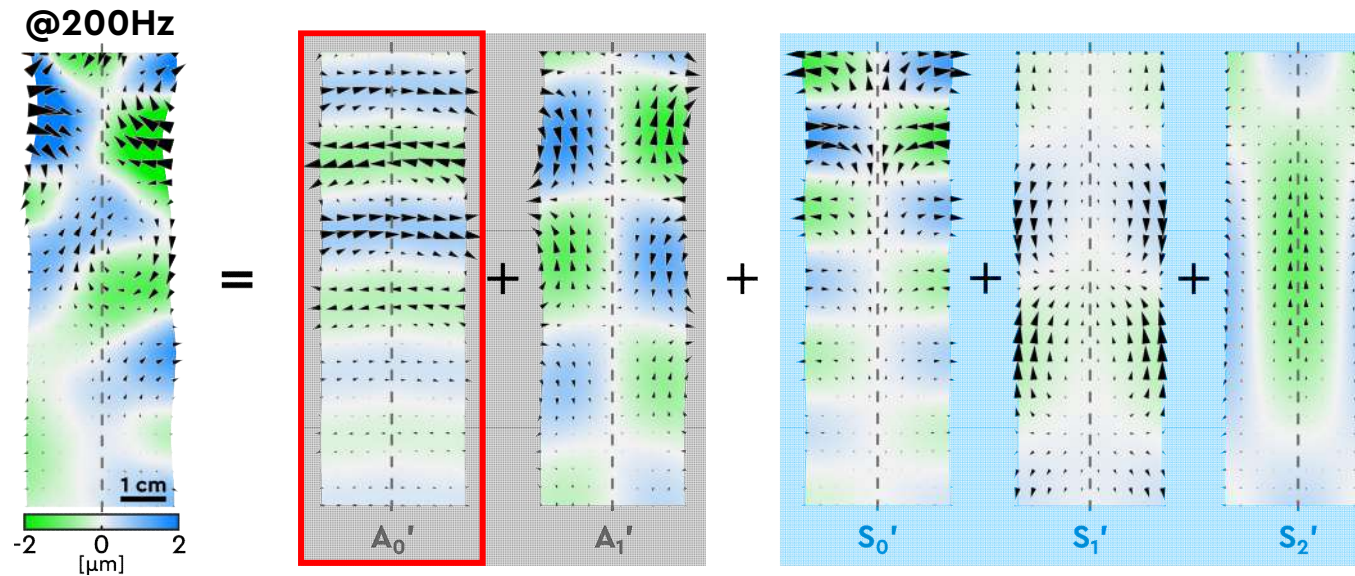
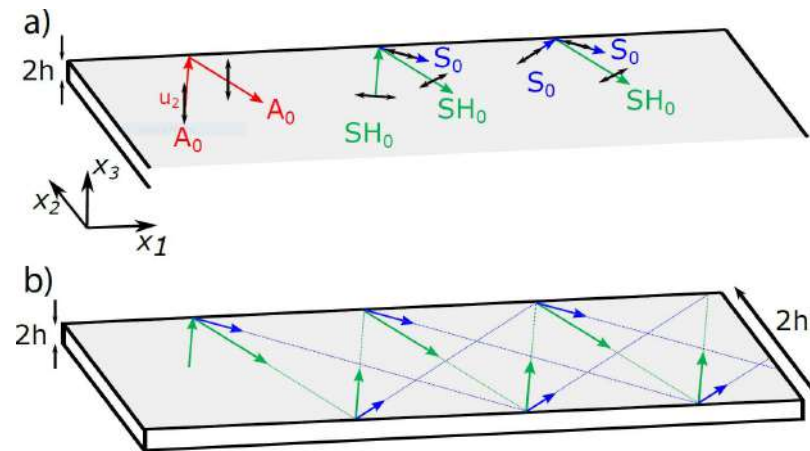
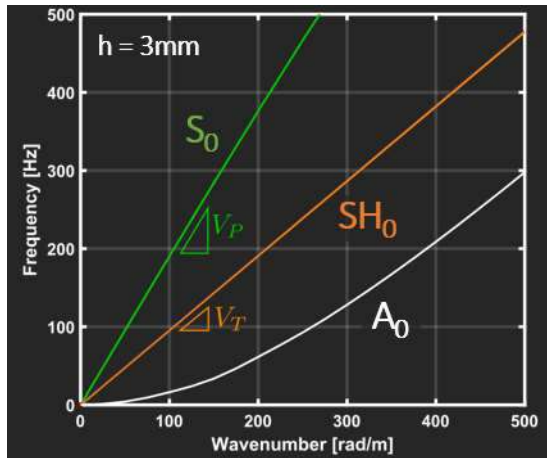


# First observations in the strip configuration



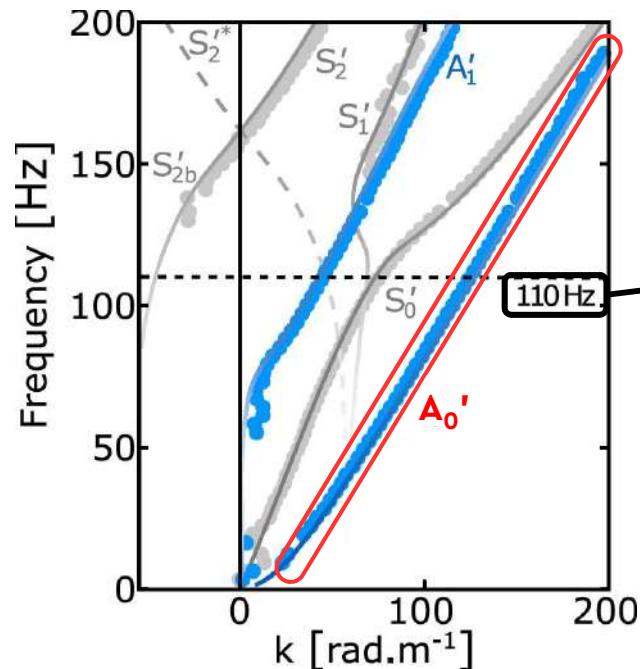
field  $s(x_1, t)$  for one push





Delory, Lemoult, Lanoy, Eddi & Prada. "Soft elastomers: A playground for guided waves", JASA **151** (2022)

Delory, Kiefer, Lanoy, Eddi, Prada & Lemoult. "Guided elastic waves in deformed viscoelastic strips", Soft Matter **in prep** (2023)



At low frequency:  
Flexural wave

At high frequency:  
Pseudo-Rayleigh wave

Many interesting waves features ! Such as:

- backward waves
- linear crossing at  $k = 0$
- ZGV in a viscoelastic solid

...

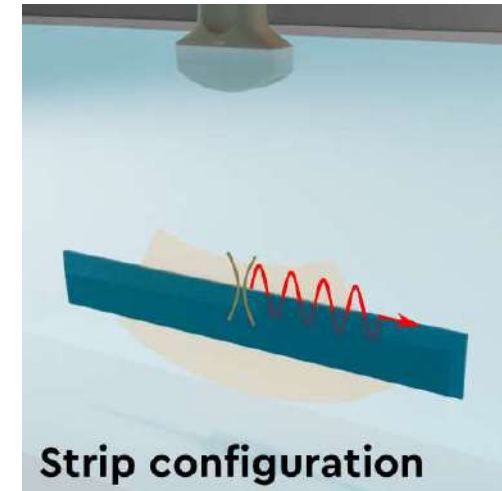
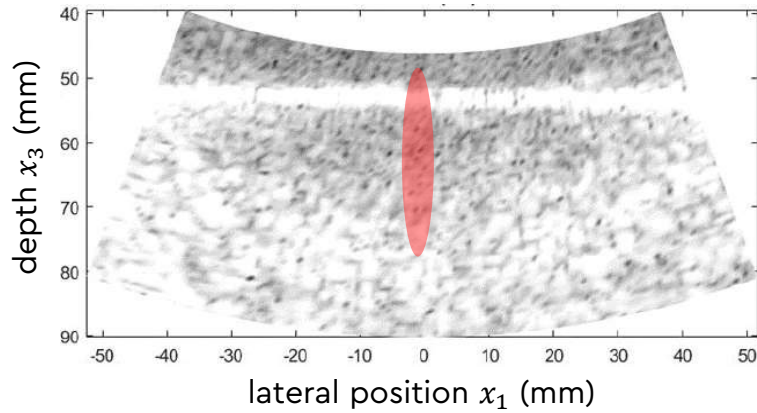
Lanoy, Lemoult, Eddi & Prada. "Dirac cones and chiral selection of elastic waves in a soft strip", PNAS **117**, 48 (2020)

Delory, Lemoult, Lanoy, Eddi & Prada. "Soft elastomers: A playground for guided waves", JASA **151** (2022)

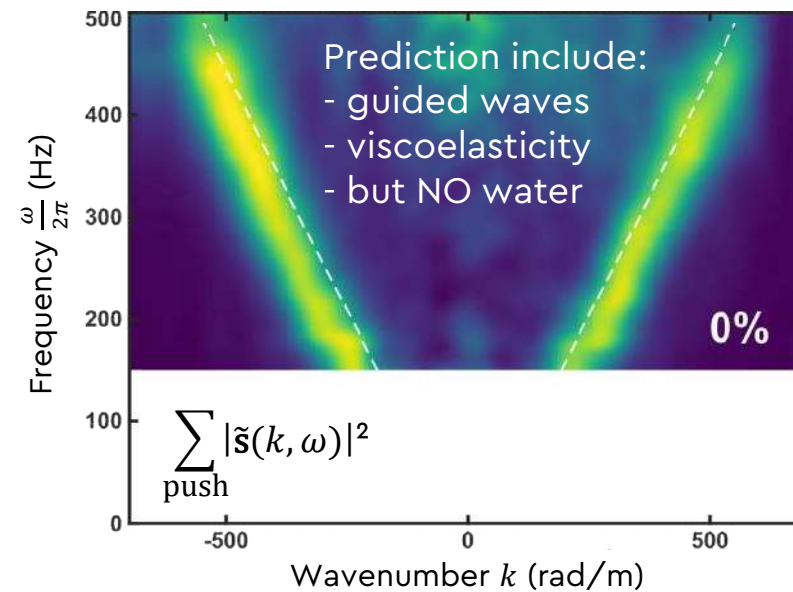
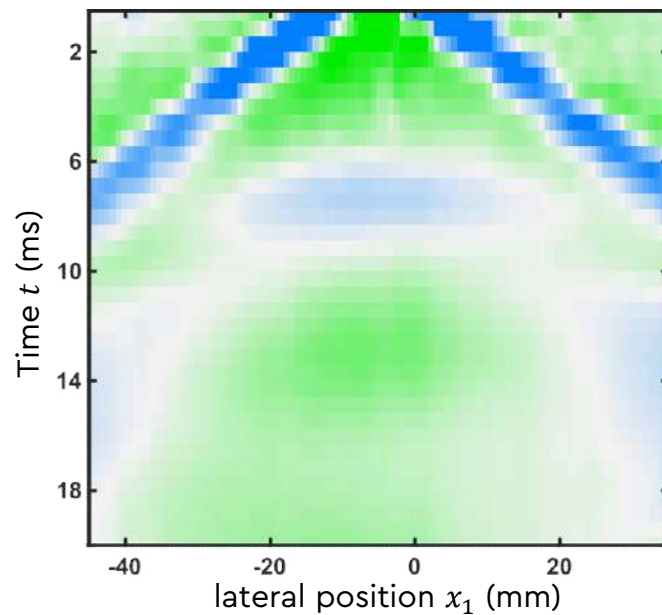


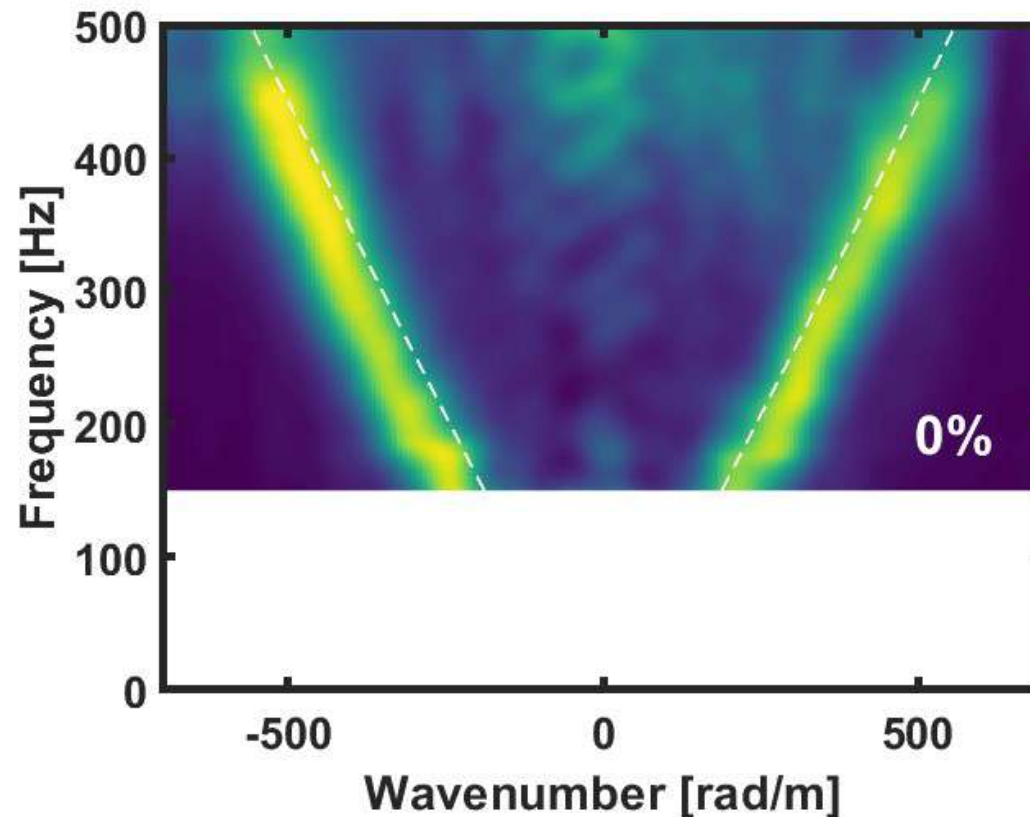


Typical reconstructed image



field  $s(x_1, t)$  for one push





- Prediction include:
- guided waves
  - viscoelasticity
  - but NO water
  - deformation

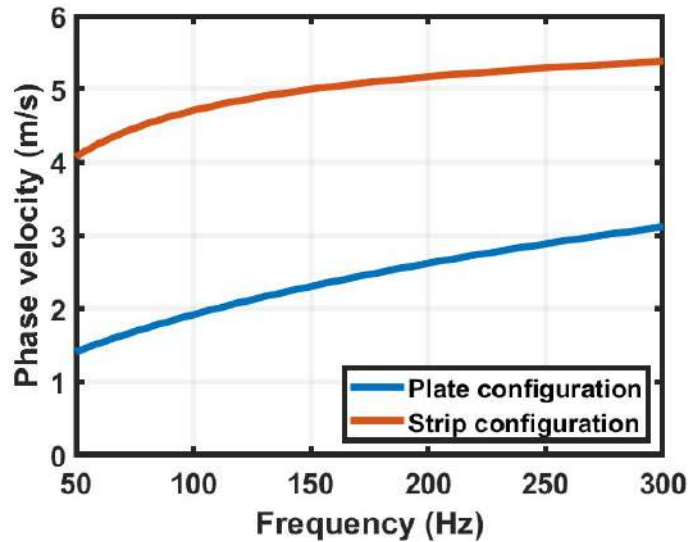
To sum up, in the **SAME STRIP**, we measured velocities:

- at different frequencies
- with different orientations
- for different deformations

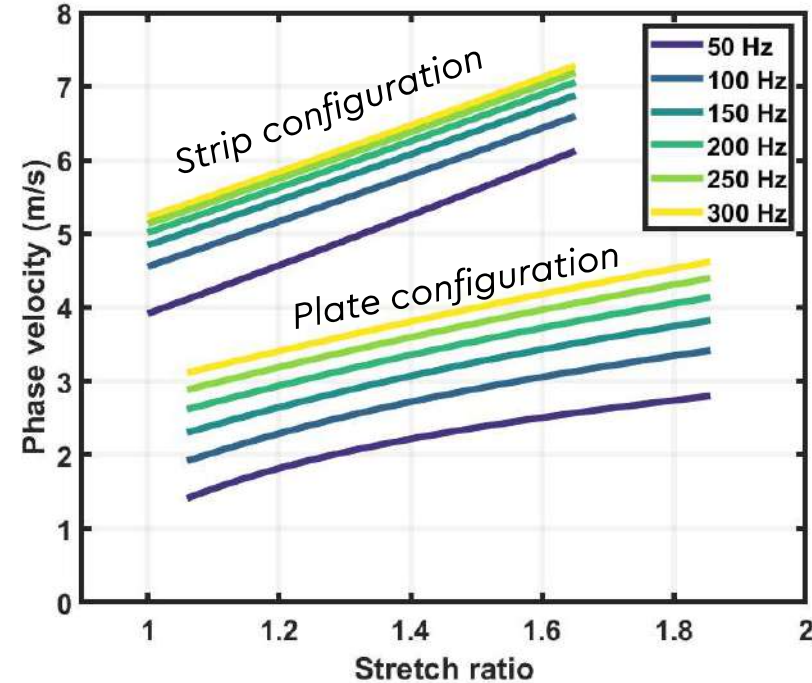
→ **Let's now compare everything**



Effect of the frequency and orientation



Effect of the deformation



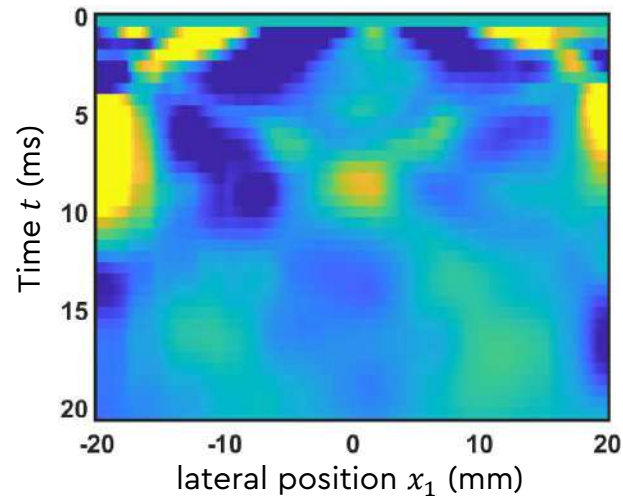
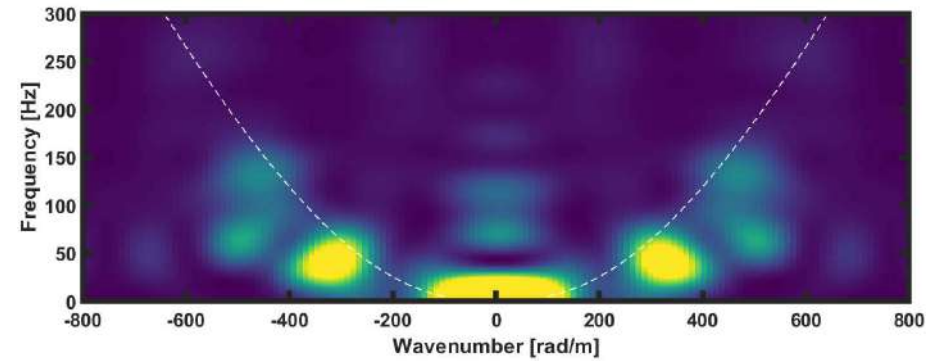
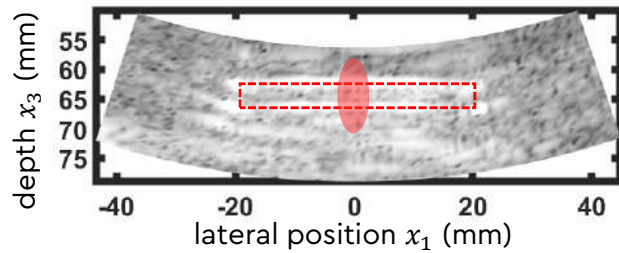
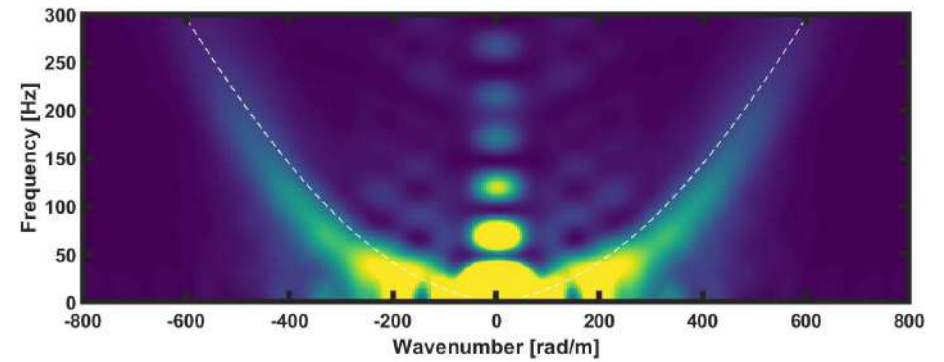
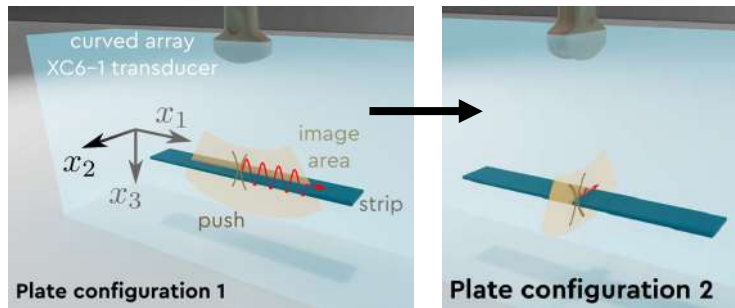
## CONCLUSIONS:

From a physical point of view:

An efficient method to observe and study (guided) elastic waves in deformed soft solids

From a medical point of view:

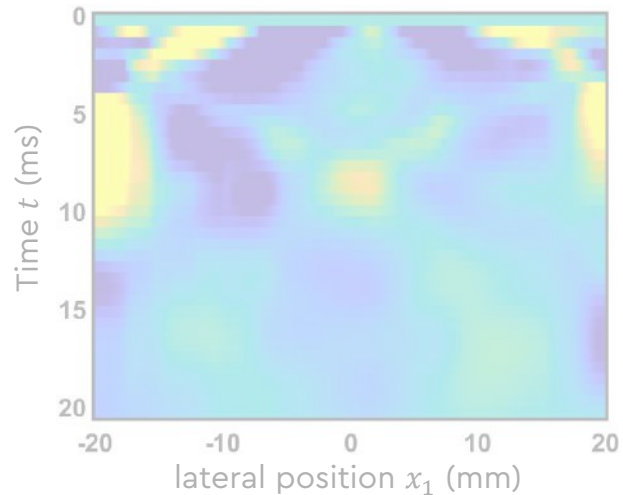
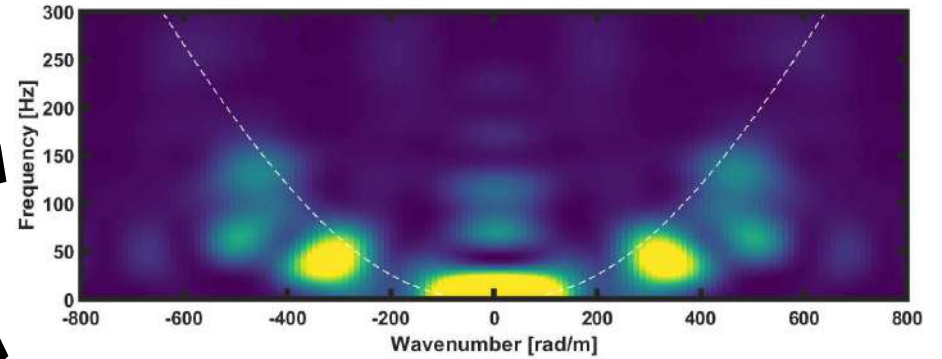
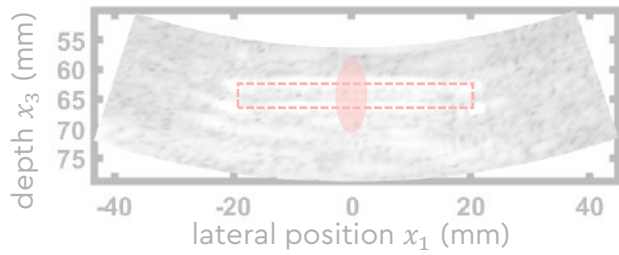
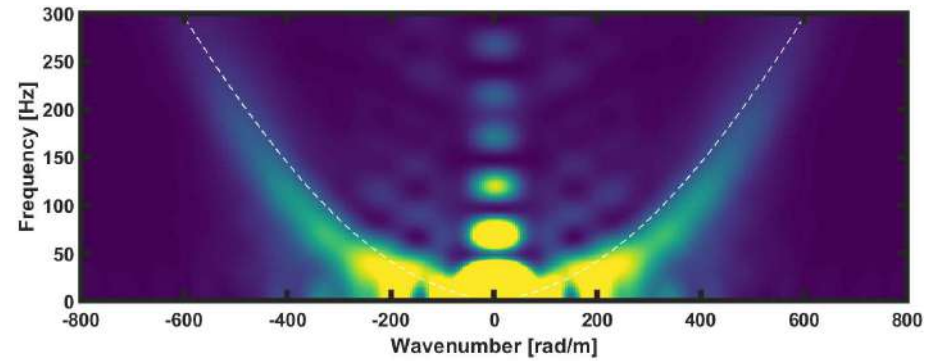
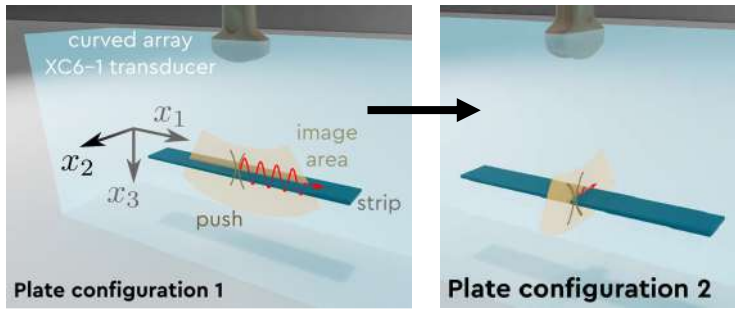
The initial assumption leads to differences of up to a factor **20** in the evaluation of Young Modulus



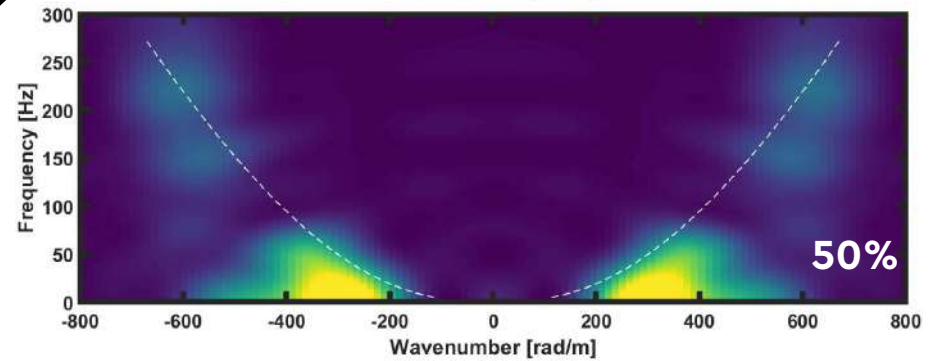




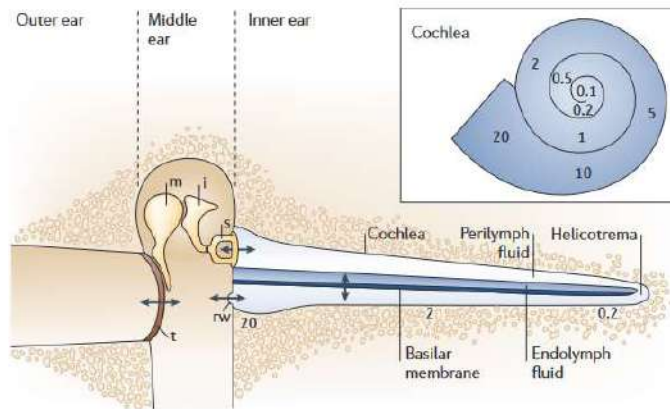
# Another surprising result



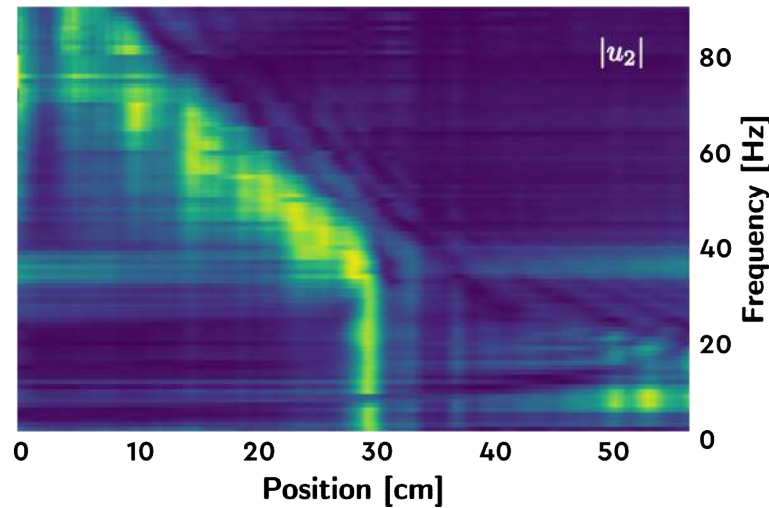
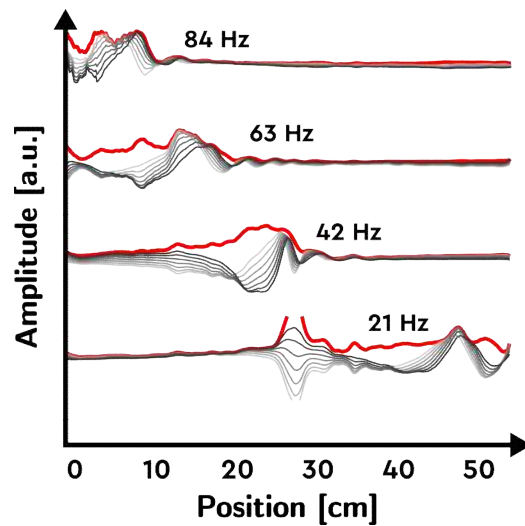
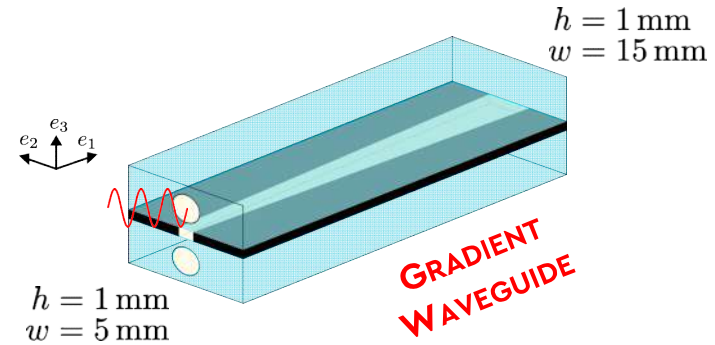
Pierre Chantelot



Cut-off wavenumber: elastic instability ?



Our macroscopic cochlea model:



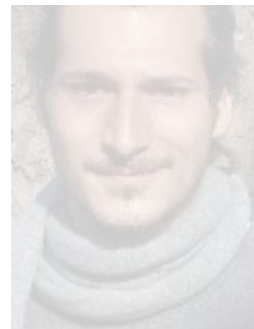
Samuel Croquette



# Elastography in deformed viscoelastic strips

**Thank you for your attention !**

A. DELORY<sup>1,2</sup>, D. KIEFER<sup>1</sup>, M. LANOY<sup>1,3</sup>, A. EDDI<sup>2</sup>, C. PRADA<sup>1</sup> & F. LEMOULT<sup>1</sup>



GdR MecaWave – May 9, 2022

<sup>1</sup> Institut Langevin, ESPCI Paris, Université PSL, CNRS, Paris, France

<sup>2</sup> PMMH, ESPCI Paris, Université PSL, Sorbonne Université, Paris

<sup>3</sup> LAUM, IA-GS, CNRS, Le Mans Université, Le Mans, France